

Parsing with CFGs

L545
Dept. of Linguistics, Indiana University
Spring 2013

Parsing with CFGs

Direction of processing
Top-down
Bottom-up
Left-corner parsing
Chart parsing
CYK
Earley

Parsing with CFGs: Overview

Input: a string

Output: a (single) parse tree

- ▶ A useful step in the process of obtaining meaning
- ▶ We can view the problem as searching through all possible parses (tree structures) to find the right one

Strategies:

- ▶ top-down (goal-directed) vs. bottom-up (data-directed)
- ▶ depth-first vs. breadth-first
- ▶ left-corner parsing (adding bottom-up to top-down)
- ▶ chart parsing (saving partial results)

Parsing with CFGs

Direction of processing
Top-down
Bottom-up
Left-corner parsing
Chart parsing
CYK
Earley

Parsers and criteria to evaluate them

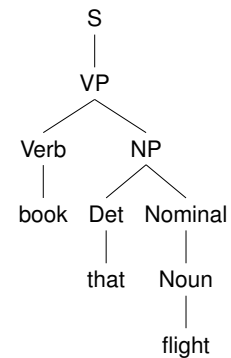
- ▶ **Function of a parser:**
 - ▶ grammar + string → analysis trees
- ▶ **Main criteria for evaluating parsers:**
 - ▶ **Correctness:** for every grammar and for every string, every analysis returned by parser is an actual analysis
 - ▶ Correctness w.r.t. our target language is thus dependent upon the grammar we give the parser
 - ▶ **Completeness:** for every grammar and for every string, every correct analysis is found by the parser
 - ▶ For large grammars, this may not be practical, and for some situations, we may want only one analysis
 - ▶ **Efficiency:** storing partial parses is essential in being efficient (to be explained)

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Direction of processing
Top-down
Bottom-up
Left-corner parsing
Chart parsing
CYK
Earley

Example grammar and desired tree

- ▶ $S \rightarrow NP VP$
- ▶ $S \rightarrow Aux NP VP$
- ▶ $S \rightarrow VP$
- ▶ $NP \rightarrow Det Nominal$
- ▶ $Nominal \rightarrow Noun$
- ▶ $Nominal \rightarrow Noun Nominal$
- ▶ $Nominal \rightarrow Nominal PP$
- ▶ $NP \rightarrow Proper-Noun$
- ▶ $VP \rightarrow Verb$
- ▶ $VP \rightarrow Verb NP$



Parsing with CFGs

Direction of processing
Top-down
Bottom-up
Left-corner parsing
Chart parsing
CYK
Earley

Direction of processing I

Top-down

Goal-driven processing is top-down:

- ▶ Start with the start symbol
- ▶ Derive sentential forms
 - ▶ If the string is among the sentences derived this way, it is part of the language

Problem: Left-recursive rules (e.g., $NP \rightarrow NP PP$) can give rise to infinite hypotheses

- ▶ Plus, we can expand non-terminals which cannot lead to the existing input
- ▶ No tree takes the properties of the lexical items into account until the last stage

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Direction of processing
Top-down
Bottom-up
Left-corner parsing
Chart parsing
CYK
Earley

How are alternatives explored?

I. Depth-first

At every choice point: Pursue a single alternative completely before trying another alternative

- ▶ State of affairs at the choice points needs to be remembered. Choices can be discarded after unsuccessful exploration.
- ▶ Depth-first search is not necessarily complete.

Problem for top-down, left-to-right, depth-first processing:

- ▶ left-recursion
For example, a rule like $N' \rightarrow N' PP$ leads to non-termination.

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Direction of processing
Top-down
Bottom-up
Left-corner parsing
Chart parsing
CYK
Earley

How are alternatives explored?

II. Breadth-first

At every choice point: Pursue every alternative for one step at a time

- Requires serious bookkeeping since each alternative computation needs to be remembered at the same time.
- Search is guaranteed to be complete.

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Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

CYK

Earley

An example grammar

Lexicon:
 Vt → saw
 Det → the
 Det → a
 N → dragon
 N → boy
 Adj → young

Syntactic rules:
 S → NP VP
 VP → Vt NP
 NP → Det N
 N → Adj N

Parsing with CFGs

Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

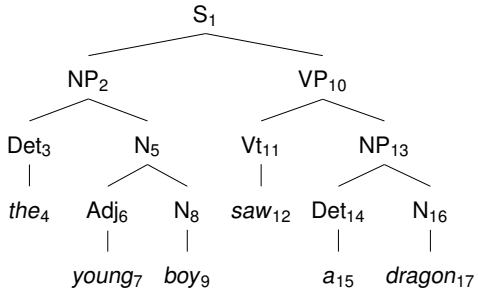
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Top-down, left-right, depth-first tree traversal

S → NP VP
 VP → Vt NP
 NP → Det N
 N → Adj N
 Vt → saw

Det → the
 Det → a
 N → dragon
 N → boy
 Adj → young



Parsing with CFGs

Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

CYK

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A walk-through

| Goal | Input | Action |
|------------|------------------------------|-------------------------------------|
| S | the young boy saw the dragon | expand S |
| NP VP | the young boy saw the dragon | expand NP |
| Det N VP | the young boy saw the dragon | expand Det |
| the N VP | the young boy saw the dragon | consume <i>the</i> |
| N VP | young boy saw the dragon | expand N |
| dragon VP | young boy saw the dragon | fail with <i>dragon</i> |
| boy VP | young boy saw the dragon | fail with <i>boy</i> ; (re)expand N |
| Adj N VP | young boy saw the dragon | expand Adj |
| young N VP | young boy saw the dragon | consume <i>young</i> |
| N VP | boy saw the dragon | expand N |

Parsing with CFGs

Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

CYK

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A walk-through (cont.)

| Goal | Input | Action |
|-----------|--------------------|-------------------------|
| dragon VP | boy saw the dragon | fail with <i>dragon</i> |
| boy VP | boy saw the dragon | consume <i>boy</i> |
| VP | saw the dragon | expand VP |
| Vt NP | saw the dragon | expand Vt |
| saw NP | saw the dragon | consume <i>saw</i> |
| NP | the dragon | expand NP |
| Det N | the dragon | expand Det |
| the N | the dragon | consume <i>the</i> |
| N | dragon | expand N |
| dragon | dragon | consume <i>dragon</i> |
| <empty> | <empty> | SUCCESS! |

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Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

CYK

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Remaining choices

- There are still some choices that have to be made:
- Which leaf node should be expanded first?
 - Left-to-right strategy moves through the leaf nodes in a left-to-right fashion
 - Which rule should be applied first for multiple rules with same LHS?
 - Can just use the textual order of rules from the grammar
 - There may be reasons to take rules in a particular order (e.g., probabilities)

Parsing with CFGs

Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

CYK

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Parsing with an agenda

- Search states are kept in an agenda
- Search states consist of partial trees and a pointer to the next input word in the sentence
- Based on what we've seen before, apply the next item on the agenda to the current tree
- Add new items to the agenda, based on the rules in the grammar which can expand at the (leftmost) node
 - We maintain the depth-first strategy by adding new hypotheses (rules) to the front of the agenda
 - If we added them to the back, we would have a breadth-first strategy

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CYK
 Earley

Direction of processing II

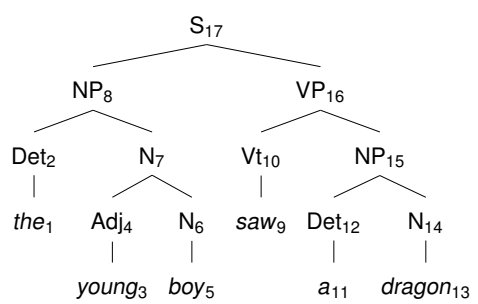
Bottom-up

- Data-driven** processing is bottom-up:
- Start with the sentence.
 - For each substring, find a grammar rule which covers it.
 - If you finish with a sentence, it is grammatical.
- Problem: Epsilon rules ($N \rightarrow \epsilon$) allow us to hypothesize empty categories anywhere in the sentence.
- Also, while any parse in progress is tied to the input, many may not lead to an S!

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CYK
 Earley

Bottom-up, left-right, depth-first tree traversal

- $S \rightarrow NP VP$
 $VP \rightarrow Vt NP$
 $NP \rightarrow Det N$
 $N \rightarrow Adj N$
 $Vt \rightarrow saw$
 $Det \rightarrow the$
 $Det \rightarrow a$
 $N \rightarrow dragon$
 $N \rightarrow boy$
 $Adj \rightarrow young$



Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CYK
 Earley

A walk-through

| Analysis | Input | Action |
|-------------|------------------------------|---|
| <empty> | the young boy saw the dragon | shift <i>the</i> |
| the | young boy saw the dragon | reduce <i>the</i> to Det |
| Det | young boy saw the dragon | shift <i>young</i> after failing to reduce Det |
| Det young | boy saw the dragon | reduce <i>young</i> to Adj after failing to reduce Det <i>young</i> |
| Det Adj | boy saw the dragon | shift <i>boy</i> |
| Det Adj boy | saw the dragon | reduce <i>boy</i> to N |
| Det Adj N | saw the dragon | reduce Adj N to N |
| Det N | saw the dragon | reduce Det N to NP |
| NP | saw the dragon | shift <i>saw</i> |

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CYK
 Earley

A walk-through (cont.)

| Analysis | Input | Action |
|------------------|------------|---------------------------|
| NP saw | the dragon | reduce <i>saw</i> to Vt |
| NP Vt | the dragon | shift <i>the</i> |
| NP Vt the | dragon | reduce <i>the</i> to Det |
| NP Vt Det | dragon | shift <i>dragon</i> |
| NP Vt Det dragon | <empty> | reduce <i>dragon</i> to N |
| NP Vt Det N | <empty> | reduce Det N to NP |
| NP Vt NP | <empty> | reduce Vt NP to VP |
| NP VP | <empty> | reduce NP VP to S |
| S | <empty> | SUCCESS! |

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CYK
 Earley

Left-corner parsing

- Motivation:
- Both pure top-down & bottom-up approaches are inefficient
 - The correct top-down parse has to be consistent with the left-most word of the input
- Left-corner parsing:** a way of using bottom-up constraints as part of a top-down strategy.
- Left-corner rule:
 - expand a node with a grammar rule only if the current input can serve as the left corner from this rule
 - Left-corner from a rule: first word along the left edge of a derivation from the rule
- Put the left-corners into a table, which then guide parsing

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CYK
 Earley

Grammar with left-corners

| | | |
|-----------------|-------------------------|----------------------|
| Lexicon: | Syntactic rules: | Left corners: |
| Vt → saw | S → NP VP | S ⇒ Det |
| Det → the | VP → Vt NP | VP ⇒ Vt |
| Det → a | NP → Det N | NP ⇒ Det |
| N → dragon | N → Adj N | N ⇒ Adj |
| N → boy | | |
| Adj → young | | |

Parsing with CFGs

Direction of processing
Top-down
Bottom-up

Left-corner parsing

Chart parsing
CYK
Earley

Left corner parsing example

Consider again *book that flight*, with these rules:

S → NP VP Nom. → Noun VP → Verb
 S → Aux NP VP Nom. → Noun Nom. VP → Verb NP
 S → VP Nom. → Nom. PP
 NP → Det Nom. NP → Proper-Noun

With an ambiguous word like *book*, left corners tell us the Noun reading is ruled out—it cannot start an S

S ⇒ Aux S ⇒ Verb VP ⇒ Verb
 S ⇒ Det NP ⇒ Det
 S ⇒ PropN NP ⇒ PropN

Moving top-down, we hypothesize S → NP VP, but the NP's left-corner is incompatible with any category of *book*

- ▶ Thus, no NP expansions are considered

Parsing with CFGs

Direction of processing
Top-down
Bottom-up

Left-corner parsing

Chart parsing
CYK
Earley

Chart parsing

Problem: Inefficiency of recomputing subresults

Two example sentences and their potential analysis:

- (1) He [gave [the young cat] [to Bill]].
- (2) He [gave [the young cat] [some milk]].

The corresponding grammar rules:

- ▶ VP → V_{ditrans} NP PP_{to}
- ▶ VP → V_{ditrans} NP NP

Regardless of final sentence analysis, the object NP (*the young cat*) will have the same analysis

⇒ No need to analyze it twice

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Direction of processing
Top-down
Bottom-up

Left-corner parsing

Chart parsing
CYK
Earley

Solution: Chart Parsing (Memoization)

- ▶ Store intermediate results:
 - a) completely analyzed constituents: **well-formed substring table** or **(passive) chart**
 - b) partial and complete analyses: **(active) chart**
- ▶ In other words, instead of recalculating that *the young cat* is an NP, we'll store that information
 - ▶ Dynamic programming: never go backwards
- ▶ All intermediate results need to be stored for completeness.
- ▶ All possible solutions are explored in parallel.

Parsing with CFGs

Direction of processing
Top-down
Bottom-up

Left-corner parsing

Chart parsing
CYK
Earley

Cocke Younger Kasami (CYK) Algorithm

- ▶ Grammar has to be in Chomsky Normal Form (CNF):
 - ▶ RHS with a single terminal: A → a
 - ▶ RHS with two non-terminals: A → BC
 - ▶ no ε rules (A → ε)
- ▶ A representation of the string showing positions and word indices:

·₀ w₁ ·₁ w₂ ·₂ w₃ ·₃ w₄ ·₄ w₅ ·₅ w₆ ·₆

For example:

·₀ the ·₁ young ·₂ boy ·₃ saw ·₄ the ·₅ dragon ·₆

Parsing with CFGs

Direction of processing
Top-down
Bottom-up

Left-corner parsing

Chart parsing
CYK
Earley

Well-formed substring table (passive chart)

- ▶ The well-formed substring table, henceforth (passive) chart, for a string of length *n* is an *n* × *n* matrix.
- ▶ The field (*i, j*) of the chart encodes the set of all categories of constituents that start at position *i* and end at position *j*, i.e.
 - ▶ chart(*i, j*) = {A | A ⇒* w_{*i*+1} ... w_{*j*}}
- ▶ The matrix is triangular since no constituent ends before it starts.

Parsing with CFGs

Direction of processing
Top-down
Bottom-up

Left-corner parsing

Chart parsing
CYK
Earley

Coverage Represented in the Chart

An input sentence with 6 words:

$\cdot_0 W_1 \cdot_1 W_2 \cdot_2 W_3 \cdot_3 W_4 \cdot_4 W_5 \cdot_5 W_6 \cdot_6$

Coverage represented in the chart:

| | | | | | | | |
|-------|---|-----|-----|-----|-----|-----|-----|
| | | TO: | | | | | |
| | | 1 | 2 | 3 | 4 | 5 | 6 |
| FROM: | 0 | 0-1 | 0-2 | 0-3 | 0-4 | 0-5 | 0-6 |
| | 1 | | 1-2 | 1-3 | 1-4 | 1-5 | 1-6 |
| | 2 | | | 2-3 | 2-4 | 2-5 | 2-6 |
| | 3 | | | | 3-4 | 3-5 | 3-6 |
| | 4 | | | | | 4-5 | 4-6 |
| | 5 | | | | | | 5-6 |

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CKY
 Earley

Example for Coverage Represented in Chart

Example sentence:

\cdot_0 the \cdot_1 young \cdot_2 boy \cdot_3 saw \cdot_4 the \cdot_5 dragon \cdot_6

Coverage represented in chart:

| | | | | | | | |
|---|-----|-----------|---------------|-------------------|-----------------------|------------------------------|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| 0 | the | the young | the young boy | the young boy saw | the young boy saw the | the young boy saw the dragon | |
| 1 | | young | young boy | young boy saw | young boy saw the | young boy saw the dragon | |
| 2 | | | boy | boy saw | boy saw the | boy saw the dragon | |
| 3 | | | | saw | saw the | saw the dragon | |
| 4 | | | | | the | the dragon | |
| 5 | | | | | | dragon | |

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CKY
 Earley

Parsing with a Passive Chart

- ▶ The CKY algorithm is used, which:
 - ▶ explores all analyses in parallel,
 - ▶ in a bottom-up fashion, &
 - ▶ stores complete subresults
- ▶ This algorithm is used to:
 - ▶ add top-down guidance (only use rules derivable from start-symbol), but avoid left-recursion problem
 - ▶ store partial analyses

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CKY
 Earley

An Example for a Filled-in Chart

Input sentence:

\cdot_0 the \cdot_1 young \cdot_2 boy \cdot_3 saw \cdot_4 the \cdot_5 dragon \cdot_6

| | | | | | | | |
|---|-------|-------|------|--------|-------|------|---|
| | | 1 | 2 | 3 | 4 | 5 | 6 |
| 0 | {Det} | {} | {NP} | {} | {} | {S} | |
| 1 | | {Adj} | {N} | {} | {} | {} | |
| 2 | | | {N} | {} | {} | {} | |
| 3 | | | | {V, N} | {} | {VP} | |
| 4 | | | | | {Det} | {NP} | |
| 5 | | | | | | {N} | |

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CKY
 Earley

Filling in the Chart

- ▶ We build all constituents that end at a certain point before we build constituents that end at a later point.

| | | | | | | |
|---|----------|----------|----------|-----------|-----------|-----------|
| | 1 | 2 | 3 | 4 | 5 | 6 |
| 0 | 1 | 3 | 6 | 10 | 15 | 21 |
| 1 | | 2 | 5 | 9 | 14 | 20 |
| 2 | | | 4 | 8 | 13 | 19 |
| 3 | | | | 7 | 12 | 18 |
| 4 | | | | | 11 | 17 |
| 5 | | | | | | 16 |

for $j := 1$ to $\text{length}(\text{string})$
lexical_chart_fill($j - 1, j$)
 for $i := j - 2$ down to 0
 syntactic_chart_fill(i, j)

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CKY
 Earley

lexical_chart_fill(j-1,j)

- ▶ Idea: Lexical lookup. Fill the field ($j - 1, j$) in the chart with the preterminal category dominating word j .
- ▶ Realized as:

$$\text{chart}(j - 1, j) := \{X \mid X \rightarrow \text{word}_j \in P\}$$

Parsing with CFGs
 Direction of processing
 Top-down
 Bottom-up
 Left-corner parsing
 Chart parsing
 CKY
 Earley

syntactic_chart_fill(i,j)

- Idea: Perform all reduction steps using syntactic rules s.t. the reduced symbol covers the string from i to j .
- Realized as: $chart(i,j) = \left\{ A \mid \begin{array}{l} A \rightarrow BC \in P, \\ i < k < j, \\ B \in chart(i,k), \\ C \in chart(k,j) \end{array} \right\}$
- Explicit loops over every possible value of k and every context free rule:
 $chart(i,j) := \{ \}$
 for $k := i + 1$ to $j - 1$
 for every $A \rightarrow BC \in P$
 if $B \in chart(i,k)$ and $C \in chart(k,j)$ then
 $chart(i,j) := chart(i,j) \cup \{A\}$.

Parsing with CFGs

Direction of processing
 Top-down
 Bottom-up

Left-corner parsing

Chart parsing

CKY

Earley

The Complete CYK Algorithm

Input: start category S and input *string*

$n := \text{length}(\text{string})$

for $j := 1$ to n
 $chart(j - 1, j) := \{X \mid X \rightarrow \text{word}_j \in P\}$
 for $i := j - 2$ down to 0
 $chart(i, j) := \{ \}$
 for $k := i + 1$ to $j - 1$
 for every $A \rightarrow BC \in P$
 if $B \in chart(i, k)$ and $C \in chart(k, j)$ then
 $chart(i, j) := chart(i, j) \cup \{A\}$

Output: if $S \in chart(0, n)$ then accept else reject

Parsing with CFGs

Direction of processing
 Top-down
 Bottom-up

Left-corner parsing

Chart parsing

CKY

Earley

How memoization helps

If we look back to the chart for the sentence *the young boy saw the dragon*:

| | | | | | | |
|---|-------|-------|------|--------|-------|------|
| | 1 | 2 | 3 | 4 | 5 | 6 |
| 0 | {Det} | {} | {NP} | {} | {} | {S} |
| 1 | | {Adj} | {N} | {} | {} | {} |
| 2 | | | {N} | {} | {} | {} |
| 3 | | | | {V, N} | {} | {VP} |
| 4 | | | | | {Det} | {NP} |
| 5 | | | | | | {N} |

- At cell (3,6), a VP is built by combining the V at (3,4) with the NP at (4,6), based on the rule $VP \rightarrow V NP$
- Regardless of further processing, that VP is never rebuilt

Parsing with CFGs

Direction of processing
 Top-down
 Bottom-up

Left-corner parsing

Chart parsing

CKY

Earley

From CYK to Earley

- CKY algorithm:
 - explores all analyses in parallel
 - bottom-up
 - stores complete subresults
- desiderata:
 - add top-down guidance (to only use rules derivable from start-symbol), but avoid left-recursion problem of top-down parsing
 - store partial analyses (useful for rules right-hand sides longer than 2)
- Idea: also store partial results, so that the chart contains
 - passive items: complete results
 - active items: partial results

Parsing with CFGs

Direction of processing
 Top-down
 Bottom-up

Left-corner parsing

Chart parsing

CKY

Earley

Representing active chart items

- well-formed substring entry:
 $chart(i, j, A)$: from i to j there is a constituent of category A
- More elaborate data structure needed to store partial results:
 - rule considered + how far processing has succeeded
 - dotted rule:
 $i[A \rightarrow \alpha \bullet_j \beta]$
- active chart entry:
 $chart(i, j, \text{state}(A, \beta))$ Note: α is not represented
 A (incompletely) goes from i to j and can be completed by finding β

Parsing with CFGs

Direction of processing
 Top-down
 Bottom-up

Left-corner parsing

Chart parsing

CKY

Earley

Dotted rule examples

- A dotted rule represents a state in processing a rule.
 - Each dotted rule is a hypothesis:
- | | |
|--|--|
| $vp \rightarrow \bullet v\text{-ditr } np \text{ } pp\text{-to}$ | We found a <i>vp</i> if we still find a <i>v-ditr</i> , a <i>np</i> , and a <i>pp-to</i> a <i>np</i> and a <i>pp-to</i> a <i>pp-to</i> nothing |
| $vp \rightarrow v\text{-ditr } \bullet np \text{ } pp\text{-to}$ | |
| $vp \rightarrow v\text{-ditr } np \bullet pp\text{-to}$ | |
| $vp \rightarrow v\text{-ditr } np \text{ } pp\text{-to} \bullet$ | |
- The first three are **active items** (or **active edges**)
 - The last one is a **passive item/edge**

Parsing with CFGs

Direction of processing
 Top-down
 Bottom-up

Left-corner parsing

Chart parsing

CKY

Earley

The three actions in Earley's algorithm

In $i[A \rightarrow \alpha \bullet_j B \beta]$ we call B the *active constituent*.

- ▶ **Prediction:** Search all rules realizing the active constituent.
- ▶ **Scanning:** Scan over each word in the input string.
- ▶ **Completion:** Combine an active edge with each passive edge covering its active constituent.

Success state: $_0[start \rightarrow s \bullet_n]$

Parsing with CFGs

- Direction of processing
 - Top-down
 - Bottom-up
- Left-corner parsing
- Chart parsing
 - CYK
 - Earley

A closer look at the three actions Prediction

Prediction: for each $i[A \rightarrow \alpha \bullet_j B \beta]$ in chart
for each $B \rightarrow \gamma$ in rules
add $j[B \rightarrow \bullet_j \gamma]$ to chart

Prediction is the task of saying what kinds of input we expect to see

- ▶ Add a rule to the chart saying that we have not seen γ , but when we do, it will form a B
- ▶ The rule covers no input, so it goes from j to j

Such rules provide the top-down aspect of the algorithm

Parsing with CFGs

- Direction of processing
 - Top-down
 - Bottom-up
- Left-corner parsing
- Chart parsing
 - CYK
 - Earley

A closer look at the three actions Scanning

Scanning: let $w_1 \dots w_j \dots w_n$ be the input string
for each $i[A \rightarrow \alpha \bullet_{j-1} w_j \beta]$ in chart
add $i[A \rightarrow \alpha w_j \bullet_j \beta]$ to chart

Scanning reads in lexical items

- ▶ We add a dotted rule indicating that a word has been seen between $j - 1$ and j
- ▶ Such a completed dotted rule can be used to complete other dotted rules

These rules provide the bottom-up component to the algorithm

Parsing with CFGs

- Direction of processing
 - Top-down
 - Bottom-up
- Left-corner parsing
- Chart parsing
 - CYK
 - Earley

A closer look at the three actions Completion

Completion (fundamental rule of chart parsing):
for each $i[A \rightarrow \alpha \bullet_k B \beta]$ and $k[B \rightarrow \gamma \bullet_j]$ in chart
add $i[A \rightarrow \alpha B \bullet_j \beta]$ to chart

Completion combines two rules in order to move the dot, i.e., indicate that something has been seen

- ▶ A rule covering B has been seen, so any rule A which refers to B in its RHS moves the dot
- ▶ Instead of spanning from i to k , A now spans from i to j , which is where B ended

Once the dot is moved, the rule will not be created again

Parsing with CFGs

- Direction of processing
 - Top-down
 - Bottom-up
- Left-corner parsing
- Chart parsing
 - CYK
 - Earley

Eliminating scanning

Scanning: for each $i[A \rightarrow \alpha \bullet_{j-1} w_j \beta]$ in chart
add $i[A \rightarrow \alpha w_j \bullet_j \beta]$ to chart

Completion:
for each $i[A \rightarrow \alpha \bullet_k B \beta]$ and $k[B \rightarrow \gamma \bullet_j]$ in chart
add $i[A \rightarrow \alpha B \bullet_j \beta]$ to chart

Observation: Scanning = completion + words as passive edges. One can thus simplify scanning to adding a passive edge for each word:

for each w_j in $w_1 \dots w_n$
add $_{j-1}[w_j \rightarrow \bullet_j]$ to chart

Parsing with CFGs

- Direction of processing
 - Top-down
 - Bottom-up
- Left-corner parsing
- Chart parsing
 - CYK
 - Earley

Earley's algorithm without scanning

General setup:
apply prediction and completion to every item added to chart

Start: add $_0[start \rightarrow \bullet_0 s]$ to chart

for each w_j in $w_1 \dots w_n$
add $_{j-1}[w_j \rightarrow \bullet_j]$ to chart

Success state: $_0[start \rightarrow s \bullet_n]$

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A tiny example grammar

Lexicon:

- vp → left
- det → the
- n → boy
- n → girl

Syntactic rules:

- s → np vp
- np → det n

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An example run

- | | |
|---------------------|--|
| start | 1. $0[\text{start} \rightarrow \bullet_0 \text{ s}]$ |
| predict from 1 | 2. $0[\text{s} \rightarrow \bullet_0 \text{ np vp}]$ |
| predict from 2 | 3. $0[\text{np} \rightarrow \bullet_0 \text{ det n}]$ |
| predict from 3 | 4. $0[\text{det} \rightarrow \bullet_0 \text{ the}]$ |
| scan "the" | 5. $0[\text{the} \rightarrow \bullet_1]$ |
| complete 4 with 5 | 6. $0[\text{det} \rightarrow \text{the} \bullet_1]$ |
| complete 3 with 6 | 7. $0[\text{np} \rightarrow \text{det} \bullet_1 \text{ n}]$ |
| predict from 7 | 8. $1[\text{n} \rightarrow \bullet_1 \text{ boy}]$ |
| predict from 7 | 9. $1[\text{n} \rightarrow \bullet_1 \text{ girl}]$ |
| scan "boy" | 10. $1[\text{boy} \rightarrow \bullet_2]$ |
| complete 8 with 10 | 11. $1[\text{n} \rightarrow \text{boy} \bullet_2]$ |
| complete 7 with 11 | 12. $0[\text{np} \rightarrow \text{det n} \bullet_2]$ |
| complete 2 with 12 | 13. $0[\text{s} \rightarrow \text{np} \bullet_2 \text{ vp}]$ |
| predict from 13 | 14. $2[\text{vp} \rightarrow \bullet_2 \text{ left}]$ |
| scan "left" | 15. $2[\text{left} \rightarrow \bullet_3]$ |
| complete 14 with 15 | 16. $2[\text{vp} \rightarrow \text{left} \bullet_3]$ |
| complete 13 with 16 | 17. $0[\text{s} \rightarrow \text{np vp} \bullet_3]$ |
| complete 1 with 17 | 18. $0[\text{start} \rightarrow \text{s} \bullet_3]$ |

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Improving the efficiency of lexical access

- ▶ In the setup just described:
 - ▶ Words are stored as passive items so that prediction is used for preterminal categories
 - ▶ Set of predicted words for a preterminal can be huge
- ▶ If each word in the grammar is introduced by a preterminal rule $\text{cat} \rightarrow \text{word}$, one can add a **passive item for each preterminal category** which can dominate the word instead of for the word itself
- ▶ What needs to be done:
 - ▶ syntactically distinguish syntactic rules from rules with preterminals on the left-hand side, i.e. lexical entries.
 - ▶ modify scanning to take lexical entries into account

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Earley parsing

- The Earley algorithm is efficient, running in polynomial time.
- ▶ Technically, however, it is a recognizer, not a parser
- To make it a parser, each state needs to be augmented with a pointer to the states that its rule covers
- ▶ For example, VP points to state where V was completed and state where NP was completed
 - ▶ Also true of the CKY algorithm: pointers need to be added to make it a parser

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