

# Parsing with CFGs

L445 / L545  
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# Parsing with CFGs: Overview

**Input:** a string

**Output:** a (single) parse tree

- ▶ A useful step in the process of obtaining meaning
- ▶ We can view the problem as searching through all possible parses (tree structures) to find the right one

**Strategies:**

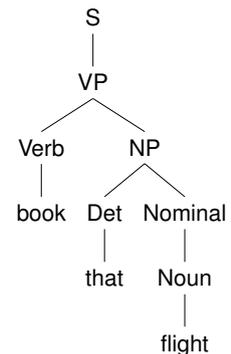
- ▶ top-down (goal-directed) vs. bottom-up (data-directed)
- ▶ depth-first vs. breadth-first
- ▶ left-corner parsing (adding bottom-up to top-down)
- ▶ chart parsing (saving partial results)

# Parsers and criteria to evaluate them

- ▶ **Function of a parser:**
  - ▶ grammar + string → analysis trees
- ▶ **Main criteria for evaluating parsers:**
  - ▶ **Correctness:** for every grammar and for every string, every analysis returned by parser is an actual analysis
    - ▶ Correctness w.r.t. our target language is thus dependent upon the grammar we give the parser
  - ▶ **Completeness:** for every grammar and for every string, every correct analysis is found by the parser
    - ▶ For large grammars, this may not be practical, and for some situations, we may want only one analysis
  - ▶ **Efficiency:** storing partial parses is essential in being efficient (to be explained)

# Example grammar and desired tree

- ▶  $S \rightarrow NP VP$
- ▶  $S \rightarrow Aux NP VP$
- ▶  $S \rightarrow VP$
- ▶  $NP \rightarrow Det Nominal$
- ▶  $Nominal \rightarrow Noun$
- ▶  $Nominal \rightarrow Noun Nominal$
- ▶  $Nominal \rightarrow Nominal PP$
- ▶  $NP \rightarrow Proper-Noun$
- ▶  $VP \rightarrow Verb$
- ▶  $VP \rightarrow Verb NP$



# Direction of processing I

Top-down

**Goal-driven** processing is top-down:

- ▶ Start with the start symbol
- ▶ Derive sentential forms
  - ▶ If the string is among the sentences derived this way, it is part of the language

Problem: Left-recursive rules (e.g.,  $NP \rightarrow NP PP$ ) can give rise to infinite hypotheses

- ▶ Plus, we can expand non-terminals which cannot lead to the existing input
- ▶ No tree takes the properties of the lexical items into account until the last stage

# How are alternatives explored?

I. Depth-first

At every choice point: Pursue a single alternative completely before trying another alternative

- ▶ State of affairs at the choice points needs to be remembered. Choices can be discarded after unsuccessful exploration.
- ▶ Depth-first search is not necessarily complete.

Problem for top-down, left-to-right, depth-first processing:

- ▶ left-recursion  
For example, a rule like  $N' \rightarrow N' PP$  leads to non-termination.

# How are alternatives explored?

## II. Breadth-first

At every choice point: Pursue every alternative for one step at a time

- Requires serious bookkeeping since each alternative computation needs to be remembered at the same time.
- Search is guaranteed to be complete.

Parsing with CFGs

Direction of processing

Top-down

Bottom-up

Left-corner parsing

Chart parsing

CYK

Earley

# An example grammar

**Lexicon:**  
 Vt → saw  
 Det → the  
 Det → a  
 N → dragon  
 N → boy  
 Adj → young

**Syntactic rules:**  
 S → NP VP  
 VP → Vt NP  
 NP → Det N  
 N → Adj N

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Chart parsing

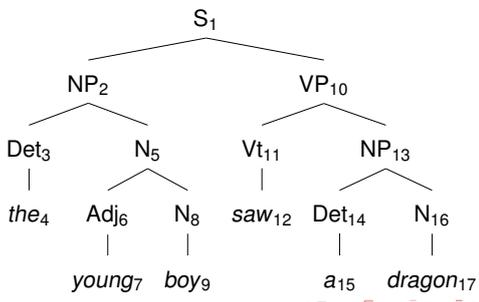
CYK

Earley

# Top-down, left-right, depth-first tree traversal

S → NP VP  
 VP → Vt NP  
 NP → Det N  
 N → Adj N  
 Vt → saw

Det → the  
 Det → a  
 N → dragon  
 N → boy  
 Adj → young



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# A walk-through

Goal	Input	Action
S	the young boy saw the dragon	expand S
NP VP	the young boy saw the dragon	expand NP
Det N VP	the young boy saw the dragon	expand Det
the N VP	the young boy saw the dragon	consume <i>the</i>
N VP	young boy saw the dragon	expand N
dragon VP	young boy saw the dragon	fail with <i>dragon</i>
boy VP	young boy saw the dragon	fail with <i>boy</i> ; (re)expand N
Adj N VP	young boy saw the dragon	expand Adj
young N VP	young boy saw the dragon	consume <i>young</i>
N VP	boy saw the dragon	expand N

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# A walk-through (cont.)

Goal	Input	Action
dragon VP	boy saw the dragon	fail with <i>dragon</i>
boy VP	boy saw the dragon	consume <i>boy</i>
VP	saw the dragon	expand VP
Vt NP	saw the dragon	expand Vt
saw NP	saw the dragon	consume <i>saw</i>
NP	the dragon	expand NP
Det N	the dragon	expand Det
the N	the dragon	consume <i>the</i>
N	dragon	expand N
dragon	dragon	consume <i>dragon</i>
<empty>	<empty>	SUCCESS!

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# Remaining choices

- There are still some choices that have to be made:
- Which leaf node should be expanded first?
    - Left-to-right strategy moves through the leaf nodes in a left-to-right fashion
  - Which rule should be applied first for multiple rules with same LHS?
    - Can just use the textual order of rules from the grammar
    - There may be reasons to take rules in a particular order (e.g., probabilities)

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# Parsing with an agenda

- Search states are kept in an agenda
- Search states consist of partial trees and a pointer to the next input word in the sentence
- Based on what we've seen before, apply the next item on the agenda to the current tree
- Add new items to the agenda, based on the rules in the grammar which can expand at the (leftmost) node
    - We maintain the depth-first strategy by adding new hypotheses (rules) to the front of the agenda
    - If we added them to the back, we would have a breadth-first strategy

# Direction of processing II

Bottom-up

Data-driven processing is bottom-up:

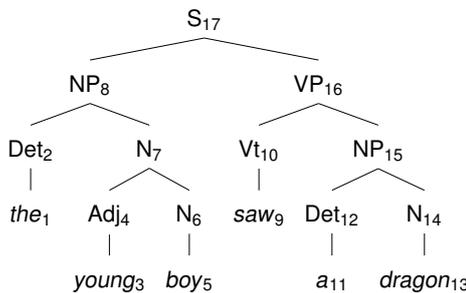
- Start with the sentence.
- For each substring, find a grammar rule which covers it.
- If you finish with a sentence, it is grammatical.

Problem: Epsilon rules ( $N \rightarrow \epsilon$ ) allow us to hypothesize empty categories anywhere in the sentence.

- Also, while any parse in progress is tied to the input, many may not lead to an S!

# Bottom-up, left-right, depth-first tree traversal

- $S \rightarrow NP VP$   
 $VP \rightarrow Vt NP$   
 $NP \rightarrow Det N$   
 $N \rightarrow Adj N$   
 $Vt \rightarrow saw$   
 $Det \rightarrow the$   
 $Det \rightarrow a$   
 $N \rightarrow dragon$   
 $N \rightarrow boy$   
 $Adj \rightarrow young$



# A walk-through

Analysis	Input	Action
<empty>	the young boy saw the dragon	shift <i>the</i>
the	young boy saw the dragon	reduce <i>the</i> to Det
Det	young boy saw the dragon	shift <i>young</i> after failing to reduce Det
Det young	boy saw the dragon	reduce <i>young</i> to Adj after failing to reduce Det <i>young</i>
Det Adj	boy saw the dragon	shift <i>boy</i>
Det Adj boy	saw the dragon	reduce <i>boy</i> to N
Det Adj N	saw the dragon	reduce Adj N to N
Det N	saw the dragon	reduce Det N to NP
NP	saw the dragon	shift <i>saw</i>

# A walk-through (cont.)

Analysis	Input	Action
NP saw	the dragon	reduce <i>saw</i> to Vt
NP Vt	the dragon	shift <i>the</i>
NP Vt the	dragon	reduce <i>the</i> to Det
NP Vt Det	dragon	shift <i>dragon</i>
NP Vt Det dragon	<empty>	reduce <i>dragon</i> to N
NP Vt Det N	<empty>	reduce Det N to NP
NP Vt NP	<empty>	reduce Vt NP to VP
NP VP	<empty>	reduce NP VP to S
S	<empty>	SUCCESS!

# Left-corner parsing

Motivation:

- Both pure top-down & bottom-up approaches are inefficient
- The correct top-down parse has to be consistent with the left-most word of the input

**Left-corner parsing:** a way of using bottom-up constraints as part of a top-down strategy.

- Left-corner rule:
  - Expand a node with a grammar rule only if the current input can serve as the left corner from this rule
- Left-corner from a rule: first word along the left edge of a derivation from the rule

Put the left-corners into a table, which then guide parsing

# Grammar with left-corners

<b>Lexicon:</b>	<b>Syntactic rules:</b>	<b>Left corners:</b>
Vt → saw	S → NP VP	S ⇒ Det
Det → the	VP → Vt NP	VP ⇒ Vt
Det → a	NP → Det N	NP ⇒ Det
N → dragon	N → Adj N	N ⇒ Adj
N → boy		
Adj → young		

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# Left corner parsing example

Consider again *book that flight*, with these rules:

S → NP VP          Nom. → Noun          VP → Verb  
 S → Aux NP VP      Nom. → Noun Nom.      VP → Verb NP  
 S → VP              Nom. → Nom. PP  
 NP → Det Nom.      NP → Proper-Noun

With an ambiguous word like *book*, left corners tell us the Noun reading is ruled out—it cannot start an S

S ⇒ Aux              S ⇒ Verb              VP ⇒ Verb  
 S ⇒ Det              NP ⇒ Det  
 S ⇒ PropN           NP ⇒ PropN

Moving top-down, we hypothesize S → NP VP, but the NP's left-corner is incompatible with any category of *book*

- ▶ Thus, no NP expansions are considered

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# Chart parsing

Problem: Inefficiency of recomputing subresults

Two example sentences and their potential analysis:

- (1) He [gave [the young cat] [to Bill]].
- (2) He [gave [the young cat] [some milk]].

The corresponding grammar rules:

- ▶ VP → V<sub>ditrans</sub> NP PP<sub>to</sub>
- ▶ VP → V<sub>ditrans</sub> NP NP

Regardless of final sentence analysis, the object NP (*the young cat*) will have the same analysis

⇒ No need to analyze it twice

Parsing with CFGs

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# Solution: Chart Parsing (Memoization)

- ▶ Store intermediate results:
  - a) completely analyzed constituents: **well-formed substring table** or **(passive) chart**
  - b) partial and complete analyses: **(active) chart**
- ▶ In other words, instead of recalculating that *the young cat* is an NP, we'll store that information
  - ▶ Dynamic programming: never go backwards
- ▶ All intermediate results need to be stored for completeness.
- ▶ All possible solutions are explored in parallel.

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# Cocke Younger Kasami (CYK) Algorithm

- ▶ Grammar has to be in Chomsky Normal Form (CNF):
  - ▶ RHS with a single terminal: A → a
  - ▶ RHS with two non-terminals: A → BC
  - ▶ no ε rules (A → ε)
- ▶ A representation of the string showing positions and word indices:

·<sub>0</sub> w<sub>1</sub> ·<sub>1</sub> w<sub>2</sub> ·<sub>2</sub> w<sub>3</sub> ·<sub>3</sub> w<sub>4</sub> ·<sub>4</sub> w<sub>5</sub> ·<sub>5</sub> w<sub>6</sub> ·<sub>6</sub>

For example:

·<sub>0</sub> the ·<sub>1</sub> young ·<sub>2</sub> boy ·<sub>3</sub> saw ·<sub>4</sub> the ·<sub>5</sub> dragon ·<sub>6</sub>

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# Well-formed substring table (passive chart)

- ▶ The well-formed substring table, henceforth (passive) chart, for a string of length *n* is an *n* × *n* matrix.
- ▶ The field (*i, j*) of the chart encodes the set of all categories of constituents that start at position *i* and end at position *j*, i.e.
  - ▶ chart(*i, j*) = {A | A ⇒\* w<sub>*i*+1</sub> ... w<sub>*j*</sub>}
- ▶ The matrix is triangular since no constituent ends before it starts.

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# Coverage Represented in the Chart

An input sentence with 6 words:

$\cdot_0 W_1 \cdot_1 W_2 \cdot_2 W_3 \cdot_3 W_4 \cdot_4 W_5 \cdot_5 W_6 \cdot_6$

Coverage represented in the chart:

		TO:					
		1	2	3	4	5	6
FROM:	0	0-1	0-2	0-3	0-4	0-5	0-6
	1		1-2	1-3	1-4	1-5	1-6
	2			2-3	2-4	2-5	2-6
	3				3-4	3-5	3-6
	4					4-5	4-6
	5						5-6

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# Example for Coverage Represented in Chart

Example sentence:

$\cdot_0$  the  $\cdot_1$  young  $\cdot_2$  boy  $\cdot_3$  saw  $\cdot_4$  the  $\cdot_5$  dragon  $\cdot_6$

Coverage represented in chart:

	1	2	3	4	5	6
0	the	the young	the young boy	the young boy saw	the young boy saw the	the young boy saw the dragon
1		young	young boy	young boy saw	young boy saw the	young boy saw the dragon
2			boy	boy saw	boy saw the	boy saw the dragon
3				saw	saw the	saw the dragon
4					the	the dragon
5						dragon

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# Parsing with a Passive Chart

- ▶ The CKY algorithm is used, which:
  - ▶ explores all analyses in parallel,
  - ▶ in a bottom-up fashion, &
  - ▶ stores complete subresults
- ▶ This algorithm is used to:
  - ▶ add top-down guidance (only use rules derivable from start-symbol), but avoid left-recursion problem
  - ▶ store partial analyses

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# An Example for a Filled-in Chart

Input sentence:

$\cdot_0$  the  $\cdot_1$  young  $\cdot_2$  boy  $\cdot_3$  saw  $\cdot_4$  the  $\cdot_5$  dragon  $\cdot_6$

Chart:

	1	2	3	4	5	6
0	{Det}	{}	{NP}	{}	{}	{S}
1		{Adj}	{N}	{}	{}	{}
2			{N}	{}	{}	{}
3				{V, N}	{}	{VP}
4					{Det}	{NP}
5						{N}

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# Filling in the Chart

- ▶ We build all constituents that end at a certain point before we build constituents that end at a later point.

	1	2	3	4	5	6
0	<b>1</b>	<b>3</b>	<b>6</b>	<b>10</b>	<b>15</b>	<b>21</b>
1		<b>2</b>	<b>5</b>	<b>9</b>	<b>14</b>	<b>20</b>
2			<b>4</b>	<b>8</b>	<b>13</b>	<b>19</b>
3				<b>7</b>	<b>12</b>	<b>18</b>
4					<b>11</b>	<b>17</b>
5						<b>16</b>

for  $j := 1$  to  $\text{length}(\text{string})$   
**lexical\_chart\_fill**( $j - 1, j$ )  
 for  $i := j - 2$  down to 0  
     syntactic\_chart\_fill( $i, j$ )

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# lexical\_chart\_fill(j-1,j)

- ▶ Idea: Lexical lookup. Fill the field ( $j - 1, j$ ) in the chart with the preterminal category dominating word  $j$ .
- ▶ Realized as:

$$\text{chart}(j - 1, j) := \{X \mid X \rightarrow \text{word}_j \in P\}$$

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## syntactic\_chart\_fill(i,j)

▶ Idea: Perform all reduction steps using syntactic rules s.t. the reduced symbol covers the string from  $i$  to  $j$ .

▶ Realized as: 
$$\text{chart}(i,j) = \left\{ A \mid \begin{array}{l} A \rightarrow BC \in P, \\ i < k < j, \\ B \in \text{chart}(i,k), \\ C \in \text{chart}(k,j) \end{array} \right\}$$

▶ Explicit loops over every possible value of  $k$  and every context free rule:

```
chart(i,j) := {}
for k := i + 1 to j - 1
  for every A → BC ∈ P
    if B ∈ chart(i,k) and C ∈ chart(k,j) then
      chart(i,j) := chart(i,j) ∪ {A}.
```

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## The Complete CYK Algorithm

Input: start category  $S$  and input *string*

$n := \text{length}(\text{string})$

```
for j := 1 to n
  chart(j - 1, j) := {X | X → wordj ∈ P}
  for i := j - 2 down to 0
    chart(i, j) := {}
    for k := i + 1 to j - 1
      for every A → BC ∈ P
        if B ∈ chart(i, k) and C ∈ chart(k, j) then
          chart(i, j) := chart(i, j) ∪ {A}
```

Output: if  $S \in \text{chart}(0, n)$  then accept; else reject

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## How memoization helps

If we look back to the chart for the sentence *the young boy saw the dragon*:

	1	2	3	4	5	6
0	{Det}	{}	{NP}	{}	{}	{S}
1		{Adj}	{N}	{}	{}	{}
2			{N}	{}	{}	{}
3				{V, N}	{}	{VP}
4					{Det}	{NP}
5						{N}

- ▶ At cell (3,6), a VP is built by combining the V at (3,4) with the NP at (4,6), based on the rule  $VP \rightarrow V NP$
- ▶ Regardless of further processing, that VP is never rebuilt

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## From CYK to Earley

- ▶ CKY algorithm:
  - ▶ explores all analyses in parallel
  - ▶ is bottom-up
  - ▶ stores complete subresults
- ▶ desiderata:
  - ▶ add top-down guidance (to only use rules derivable from start-symbol), but avoid left-recursion problem of top-down parsing
  - ▶ store partial analyses (useful for rules right-hand sides longer than 2)
- ▶ Idea: also store partial results, so that the chart contains
  - ▶ passive items: complete results
  - ▶ active items: partial results

Parsing with CFGs

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## Representing active chart items

- ▶ well-formed substring entry:  $\text{chart}(i, j, A)$ : from  $i$  to  $j$  there is a constituent of category  $A$
- ▶ More elaborate data structure needed to store partial results:
  - ▶ rule considered + how far processing has succeeded
  - ▶ dotted rule:  $i[A \rightarrow \alpha \bullet_j \beta]$
- ▶ active chart entry:  $\text{chart}(i, j, \text{state}(A, \beta))$  Note:  $\alpha$  is not represented  $A$  (incompletely) goes from  $i$  to  $j$  and can be completed by finding  $\beta$

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## Dotted rule examples

- ▶ A dotted rule represents a state in processing a rule.
- ▶ Each dotted rule is a hypothesis:
 

$vp \rightarrow \bullet v\text{-ditr } np \text{ } pp\text{-to}$	We found a <i>vp</i> if we still find
$vp \rightarrow v\text{-ditr } \bullet np \text{ } pp\text{-to}$	a <i>v-ditr</i> , a <i>np</i> , and a <i>pp-to</i>
$vp \rightarrow v\text{-ditr } np \bullet pp\text{-to}$	a <i>np</i> and a <i>pp-to</i>
$vp \rightarrow v\text{-ditr } np \text{ } pp\text{-to} \bullet$	a <i>pp-to</i>
	nothing

  - ▶ The first three are **active items** (or **active edges**)
  - ▶ The last one is a **passive item/edge**

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# The three actions in Earley's algorithm

In  $i[A \rightarrow \alpha \bullet_j B \beta]$  we call  $B$  the *active constituent*.

- ▶ **Prediction:** Search all rules realizing the active constituent.
- ▶ **Scanning:** Scan over each word in the input string.
- ▶ **Completion:** Combine an active edge with each passive edge covering its active constituent.

**Success state:**  $0[start \rightarrow s \bullet_n]$

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# A closer look at the three actions

## Prediction

**Prediction:** for each  $i[A \rightarrow \alpha \bullet_j B \beta]$  in chart  
for each  $B \rightarrow \gamma$  in rules  
add  $j[B \rightarrow \bullet \gamma]$  to chart

Prediction is the task of saying what kinds of input we expect to see

- ▶ Add a rule to the chart saying that we have not seen  $\gamma$ , but when we do, it will form a B
- ▶ The rule covers no input, so it goes from  $j$  to  $j$

Such rules provide the top-down aspect of the algorithm

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# A closer look at the three actions

## Scanning

**Scanning:** let  $w_1 \dots w_j \dots w_n$  be the input string  
for each  $i[A \rightarrow \alpha \bullet_{j-1} w_j \beta]$  in chart  
add  $i[A \rightarrow \alpha w_j \bullet_j \beta]$  to chart

Scanning reads in lexical items

- ▶ We add a dotted rule indicating that a word has been seen between  $j - 1$  and  $j$
- ▶ Such a completed dotted rule can be used to complete other dotted rules

These rules provide the bottom-up component to the algorithm

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# A closer look at the three actions

## Completion

### Completion (fundamental rule of chart parsing):

for each  $i[A \rightarrow \alpha \bullet_k B \beta]$  and  $k[B \rightarrow \gamma \bullet_j]$  in chart  
add  $i[A \rightarrow \alpha B \bullet_j \beta]$  to chart

Completion combines two rules in order to move the dot, i.e., indicate that something has been seen

- ▶ A rule covering B has been seen, so any rule A which refers to B in its RHS moves the dot
- ▶ Instead of spanning from  $i$  to  $k$ , A now spans from  $i$  to  $j$ , which is where B ended

Once the dot is moved, the rule will not be created again

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# Eliminating scanning

**Scanning:** for each  $i[A \rightarrow \alpha \bullet_{j-1} w_j \beta]$  in chart  
add  $i[A \rightarrow \alpha w_j \bullet_j \beta]$  to chart

**Completion:**  
for each  $i[A \rightarrow \alpha \bullet_k B \beta]$  and  $k[B \rightarrow \gamma \bullet_j]$  in chart  
add  $i[A \rightarrow \alpha B \bullet_j \beta]$  to chart

**Observation:** Scanning = completion + words as passive edges. One can thus simplify scanning to adding a passive edge for each word:

for each  $w_j$  in  $w_1 \dots w_n$   
add  $j-1[w_j \rightarrow \bullet]$  to chart

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# Earley's algorithm without scanning

## General setup:

apply prediction and completion to every item added to chart

**Start:** add  $0[start \rightarrow \bullet_0 s]$  to chart

for each  $w_j$  in  $w_1 \dots w_n$   
add  $j-1[w_j \rightarrow \bullet]$  to chart

**Success state:**  $0[start \rightarrow s \bullet_n]$

Parsing with CFGs

Direction of processing  
Top-down  
Bottom-up

Left-corner parsing

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# A tiny example grammar

Lexicon:

- vp → left
- det → the
- n → boy
- n → girl

Syntactic rules:

- s → np vp
- np → det n

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# An example run

- |  |  |
|--|--|
| <p>start<br/>                 predict from 1<br/>                 predict from 2<br/>                 predict from 3<br/>                 scan "the"<br/>                 complete 4 with 5<br/>                 complete 3 with 6<br/>                 predict from 7<br/>                 predict from 7<br/>                 scan "boy"<br/>                 complete 8 with 10<br/>                 complete 7 with 11<br/>                 complete 2 with 12<br/>                 predict from 13<br/>                 scan "left"<br/>                 complete 14 with 15<br/>                 complete 13 with 16<br/>                 complete 1 with 17</p> | <ol style="list-style-type: none"> <li>1. <math>0[start \rightarrow \bullet_0 s]</math></li> <li>2. <math>0[s \rightarrow \bullet_0 np vp]</math></li> <li>3. <math>0[np \rightarrow \bullet_0 det n]</math></li> <li>4. <math>0[det \rightarrow \bullet_0 the]</math></li> <li>5. <math>0[the \rightarrow \bullet_1]</math></li> <li>6. <math>0[det \rightarrow the \bullet_1]</math></li> <li>7. <math>0[np \rightarrow det \bullet_1 n]</math></li> <li>8. <math>1[n \rightarrow \bullet_1 boy]</math></li> <li>9. <math>1[n \rightarrow \bullet_1 girl]</math></li> <li>10. <math>1[boy \rightarrow \bullet_2]</math></li> <li>11. <math>1[n \rightarrow boy \bullet_2]</math></li> <li>12. <math>0[np \rightarrow det n \bullet_2]</math></li> <li>13. <math>0[s \rightarrow np \bullet_2 vp]</math></li> <li>14. <math>2[vp \rightarrow \bullet_2 left]</math></li> <li>15. <math>2[left \rightarrow \bullet_3]</math></li> <li>16. <math>2[vp \rightarrow left \bullet_3]</math></li> <li>17. <math>0[s \rightarrow np vp \bullet_3]</math></li> <li>18. <math>0[start \rightarrow s \bullet_3]</math></li> </ol> |
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# Improving the efficiency of lexical access

- ▶ In the setup just described:
  - ▶ Words are stored as passive items so that prediction is used for preterminal categories
  - ▶ Set of predicted words for a preterminal can be huge
- ▶ If each word in the grammar is introduced by a preterminal rule  $cat \rightarrow word$ , one can add a **passive item for each preterminal category** which can dominate the word instead of for the word itself
- ▶ What needs to be done:
  - ▶ syntactically distinguish syntactic rules from rules with preterminals on the left-hand side, i.e. lexical entries.
  - ▶ modify scanning to take lexical entries into account

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# Earley parsing

- The Earley algorithm is efficient, running in polynomial time.
- ▶ Technically, however, it is a recognizer, not a parser
- To make it a parser, each state needs to be augmented with a pointer to the states that its rule covers
- ▶ For example, VP points to state where V was completed and state where NP was completed
  - ▶ Also true of the CKY algorithm: pointers need to be added to make it a parser

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